Learning to behave via Imitation ESSAI 2024 Course Lecture 1/5

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Outline

- Day 1: Motivation & Introduction to Deep Reinforcement Learning
- Day 2: Inverse Reinforcement Learning and Connections to Probabilistic Inference
- Day 3: Imitation Learning
- Day 4: Non-Markovian, Multimodal Imitation Learning
- Day 5: Imitating in Constrained Settings, Multiagent Imitation Learning.

Imitation Learning

Learning to behave from demonstrations Examples













R.L lab @ Imperial

Imitation Learning

Problem (ambiguous) statement

Given a set of demonstrated trajectories D generated by an unknown expert policy π_{ϵ} , learn a policy π that generates trajectories that are "as close as possible" to the expert trajectories.

Imitation learning

What can go wrong?

- Lack of training data
- Noisy or erroneous training data
- Distribution mismatch
- Compounding errors
- Discrimination ability (different actions in very similar settings)
- Collapsing multi-modal behaviour in executing tasks in a single policy
- Being unaware of other agents' policies in multi-agent settings (collaborative or not)
- ... and others that will be revealed during the course

Reinforcement Learning provides a formalism for behaviour Basic Loop



Introduction to (Deep) Reinforcement Learning Reinforcement Learning provides a formalism for behaviour Examples













R.L lab @ Imperial

Reinforcement Learning provides a formalism for behaviour Basic Loop in a more rigorous way to introduce notation



What does the agent learns?

- A policy π: mapping from states S to actions P(A), based on past experience)
- Mind the dimensionality of state, action space



What does the agent learns?

- A policy π: mapping from states S to actions P(A), based on past experience)
- Mind the dimensionality of state, action space



curse of dimensionality

 $|\mathcal{S}| = (255^3)^{200 \times 200}$

(more than atoms in the universe)

Figure from P.Abeel lectures on RL

- Optimization
- Exploration
- Generalization
- Consequences and Rewards (sparse and/or delayed).

- Optimization:
 - Find an optimal way to make decisions, yielding the best outcomes or at least very good outcomes.
 In other words: Find the optimal policy π* that maximizes the sum of rewards that the agent gets while executing a task
- Exploration
- Generalization
- Consequences and Rewards (sparse and/or delayed).

- Optimization
- Exploration:
 - Learn while interacting in the world (and failing)
 - Limited interaction means limited experience and knowledge (what would have happened if..?)
 - How much curiosity should be involved in the process? What if loosing everything while learning?
- Generalization
- Consequences and Rewards (sparse and/or delayed).

- Optimization
- Exploration
- Generalization:
 - Is it possible to learn how to take optimal decisions at every possible state?
 - What about transferring decision-making knowledge between tasks?
- Consequences and Rewards (sparse and/or delayed).

- Optimization
- Exploration
- Generalization
- Consequences and Rewards (sparse and/or delayed).
 - Decisions at any particular state may have crucial impacts later on.
 - Temporal credit assignment when learning: what caused a very good or a very bad outcome?
 - Decisions when acting in the real world involve reasoning about long-term effects.

Why Deep Reinforcement Learning is important?

- Generalization abilities
- End-to-end training (what does it mean for RL)?



Why Deep Reinforcement Learning is important?

- Generalization abilities
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Why **Deep** Reinforcement Learning is important?

- Generalization abilities $\pi_{\theta}(a_t|o_t)$, a_t , r_t
- End-to-end training (what does it mean for RL)?



Advances in DRL go in par with advances in DL.



 $\begin{array}{lll} s_t \text{ state } & \pi_{\theta}(a_t|s_t) \text{ fully observable} \\ o_t \text{ observation } & \pi_{\theta}(a_t|o_t) \text{ partially observable} \\ a_t \text{ action } & r_t(s_t, a_t) \text{ reward} \end{array}$



The objective given a POMDP $(S, A, O, \mathcal{E}, \mathcal{T}, r)$, is to learn a policy that generates the best trajectories with high probability





Probability of τ given a policy π_{θ} $p_{\theta}(\tau) = p(s_1) \prod_{t=1}^{T} \pi_{\theta}(a_t|s_t) p(s_{t+1}|s_t, a_t)$

Objective: tune θ to get $\theta^* = \operatorname{argmax}_{\theta} \mathbb{E}_{\tau \sim p_{\theta}} [\sum_t r_t], r_t = r(s_t, a_t)$

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Objective: tune θ to get $\theta^* = argmax_{\theta} \mathbb{E}_{\tau \sim p_{\theta}} [\sum_t r_t], r_t = r(s_t, a_t)$

Objective for finite time horizons $\theta^* = \operatorname{argmax}_{\theta} \sum_{t=1}^{T} \mathbb{E}_{(s_t, a_t) \sim p_{\theta}(s_t, a_t)}[r_t]$, where $p_{\theta}(s_t, a_t)$ the state, action marginal

Objective for infinite time horizons

 $\theta^* = argmax_{\theta}\mathbb{E}_{(s,a)\sim\mu}[r(s,a)]$, where $\mu = p_{\theta}(s,a)$ the stationary distribution of states, actions

Definitions

- Quality of action at state $Q^{\pi}(s_t, a_t) = \sum_t^T \mathbb{E}_{\pi_{\theta}}[r(s_t, a_t)|s_t, a_t]$ Given a policy π and $Q^{\pi}(s, a)$, then we can improve π , by choosing $a = argmax_a Q^{\pi}(s, a)$
- ▶ Value of state $V^{\pi}(s_t) = \sum_t^T \mathbb{E}_{\pi_{\theta}}[r(s_t, a_t)|s_t] = \mathbb{E}_{a_t \sim \pi_{\theta}(a_t|s_t)}[Q^{\pi}(s_t, a_t)]$ In case $Q^{\pi}(s, a) > V^{\pi}(s)$ then π can be modified by increasing the probability of a.
- Advantage
 - $A^{\pi}(s_t, a_t) = \left[Q^{\pi}(s_t, a_t) V^{\pi}(s_t)\right]$

Bellman backup

$$Q^{\pi}(s,a) = r(s_t,a_t) + \mathbb{E}[(V_{t+1}^{\pi}(s_{t+1}))]$$

The anatomy of DRL algorithms

Gather samples (running a policy)

The anatomy of DRL algorithms



The anatomy of DRL algorithms



The anatomy of DRL algorithms



The anatomy of DRL algorithms: Value based



The anatomy of DRL algorithms: Q-Learning



The anatomy of DRL algorithms: Direct policy gradient





The anatomy of Q-Learning algorithms With a target network.



- 2. Choose random / policy action (a)
- Receive resulting state (s') and reward (r)
- Store all transitions (s, a, r, s') in Memory
- 5. Sample prioritized batch
- Predict Q values from Policy and Target Networks
- 7. Calculate DQN Loss
- 8. Optimize in order to minimize Loss
- 9. Periodic Target Network updates



 $L_i(\theta_i) = \mathbb{E}_{(s,a,Rwd,s') \sim U(D)}[(Rwd + \gamma max_{a'}Q(s',a'; \theta_i^-) - Q(s,a; \theta_i))^2]$

Introduction to (Deep) Reinforcement Learning The anatomy of Q-Learning algorithms Double Q Learning with target.



 $L_i(\theta_i) = \mathbb{E}_{(s,a,Rwd,s') \sim U(D)}[(Rwd + \gamma max_{a'}Q(s',a'; \theta_i^-) - Q(s,a; \theta_i))^2]$

$$Q^A(s,a) = Q^A(s,a) + lpha(Rwd + \gamma Q^B(s',a^*) - Q^A(s,a))$$

$$Y_t^{QDouble} = Rwd_{t+1} + \gamma Q(s_{t+1}, argmax_aQ(s_{t+1}, a; \ \theta_t); \ \theta_t^-)$$

So far...

- Motivation for DRL
- Notation and Definitions
- Specification of the DRL objective
- Anatomy of any DRL algorithm

Stochastic and sub-optimal behaviour

Important questions related to (D)RL

- Does (D)RL provide a reasonable model of human behaviour?
- Can we derive optimality and planning as probabilistic inference?

We need to take into account stochastic and sub-optimal behaviour











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from Y. Yue

"Strict" rationality

In any fully observed setting we can prove that there exist deterministic optimal policies, given that the objective is linear in the state, action marginals.

Recall that

• Objective for finite time horizons:

$$\theta^* = \operatorname{argmax}_{\theta} \sum_{t=1}^{T} \mathbb{E}_{(s_t, a_t) \sim p_{\theta}(s_t, a_t)} [r_t]$$

, where $p_{ heta}(s_t, a_t)$ the state, action marginal

Objective for infinite time horizons:

$$\theta^* = argmax_{\theta} \mathbb{E}_{(s,a) \sim \mu}[r(s,a)]$$

, where $\mu = p_{\theta}(s, a)$ the stationary distribution of states, actions

So we need to recover rationality to take into account randomness $_{_{36/58}}$
Introduction to (Deep) Reinforcement Learning Recovering rationality using probabilistic graphical models for sub-optimal behaviour¹



Let $p(\mathcal{O}_t|s_t, a_t) = exp(r(s_t, a_t))$, then

$$p(\tau|\mathcal{O}_{1:T}) = \frac{p(\tau, \mathcal{O}_{1:T})}{p(\mathcal{O}_{1:T})}$$
$$\propto p(\tau) \prod_{t} exp(r(s_t, a_t))$$
$$= p(\tau)exp(\sum_{t} r(s_t, a_t))$$

Any case with low reward is exponentially less likely to be chosen.

¹Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

Recovering rationality using probabilistic graphical models for sub-optimal behaviour $^{\rm 2}$

$$p(\tau|\mathcal{O}_{1:T}) = p(\tau)exp(\sum_{t} r(s_t, a_t))$$

Any case with low reward is exponentially less likely to be chosen.

- So we can model suboptimal behaviour e.g. given demonstrations of near optimal choices while performing a task (inverse and imitation learning)
- Formulates stochastic behaviour useful for exploration, generalization and transfer learning.
- We can apply inference algorithms to solve control and planning problems (under specific conditions)

²Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

Recovering rationality using probabilistic graphical models for near-optimal behaviour $^{\rm 3}$

Then we can compute the near optimal policy

$$\pi(a_t|s_t) = p(a_t|s_t, \mathcal{O}_{1:T}) = p(a_t|s_t, \mathcal{O}_{t:T}) = \frac{p(\mathcal{O}_{t:T}|s_t, a_t)}{p(\mathcal{O}_{t:T}|s_t)}p(a_t|s_t)$$
$$= \frac{\beta(s_t, a_t)}{\beta(s_t)}c$$

where, *c* is the action prior which is constant, assuming a uniform distribution, and β are backward messages computed recursively from t = T to t = 1, assuming knowledge of transition probabilities.

³Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

Recovering rationality using probabilistic graphical models for sub-optimal behaviour⁴ Given.

$$p(\mathcal{O}_t | s_t, a_t) \propto exp(r(s_t, a_t))$$
$$p(s_{t+1} | s_t, a_t)$$

Then we can compute backward messages recursively

for
$$t = T - 1$$
 to 1:

$$\beta(s_t, a_t) = p(\mathcal{O}_t | s_t, a_t) \mathbb{E}_{s_{t+1} \sim p(s_{t+1} | s_t, a_t)} [\beta_{t+1}(s_{t+1})]$$

$$\beta(s_t) = \mathbb{E}_{a_t \sim p(a_t | s_t)} [\beta(s_t, a_t)]$$

⁴Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

Introduction to (Deep) Reinforcement Learning Recovering rationality using probabilistic graphical models for sub-optimal behaviour⁵



We can also compute forward messages (useful for inverse reinforcement learning)

$$a_t(s_t) = p(s_t | \mathcal{O}_{1:t-1})$$

recursively, starting from the usually known $a_1(s_1)$, as well as the marginal probabilities

$$p(s_t|\mathcal{O}_{1:T}) \propto \beta_t(s_t)a_t(s_t)$$

⁵Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

Recovering rationality using probabilistic graphical models for sub-optimal behaviour $^{\rm 6}$

$$\beta(s_t, a_t) = p(\mathcal{O}_t | s_t, a_t) \mathbb{E}_{s_{t+1} \sim p(s_{t+1} | s_t, a_t)} [\beta_{t+1}(s_{t+1})]$$

$$\beta(s_t) = \mathbb{E}_{a_t \sim p(a_t | s_t)} [\beta(s_t, a_t)]$$

let $Q_t(s_t, a_t) = \log \beta_t(s_t, a_t) = r(s_t, a_t) + \log \mathbb{E}[\exp(V_{t+1}(s_{t+1}))]$ let $V_t(s_t) = \log \beta_t(s_t) = \log \int \exp(Q_t(s_t, a_t)) da_t$

Notice:

1. The optimistic transition implied by Q_t and

2. The softmax in the definition of $V_t(s_t)$, as $Q_t(s_t, a_t)$ gets bigger.

⁶Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

Recovering rationality using probabilistic graphical models for sub-optimal behaviour $^{7}\,$

$$\begin{aligned} Q_t(s_t, a_t) &= \log\beta_t(s_t, a_t) \\ V_t(s_t) &= \log\beta_t(s_t) \end{aligned}$$

For
$$t = T - 1$$
 to 1:
 $Q_t(s_t, a_t) = r(s_t, a_t) + \log \mathbb{E}[\exp(V_{t+1}(s_{t+1}))]$
 $V_t(s_t) = \log \int \exp(Q_t(s_t, a_t)) da_t$

 $\pi(a_t|s_t) = \frac{\beta(s_t, a_t)}{\beta(s_t)} = \exp(Q_t(s_t, a_t) - V_t(s_t)) = \exp(A_t(s_t, a_t))$ adding temperature we can balance between deterministic ($\alpha \to 0$) and stochastic (soft) ($\alpha \to \infty$) policy:

$$\pi(a_t|s_t) = \frac{\beta(s_t, a_t)}{\beta(s_t)} = \exp(\frac{1}{\alpha}Q_t(s_t, a_t) - \frac{1}{\alpha}V_t(s_t)) = \exp(\frac{1}{\alpha}A_t(s_t, a_t))$$

⁷Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

The anatomy of DRL algorithms: Soft Q-Learning with optimality bias



Variational inference⁸

То

avoid the optimistic bias of increasing the probabilities of actions that result into high rewards in very infrequent cases, we need to consider how to act near optimally given the "original" ⁹ transition probabilities.

Variational inference leads to obtaining an approximation $\hat{p}(s_{1:T}, a_{1:T})$ of $p(s_{1:T}, a_{1:T} | \mathcal{O}_{1:T})$ with dynamics $p(s_{t+1} | s_t, a_t)$

⁸Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

⁹i.e. Those not affected by our optimized decisions, $p(s_{t+1}|s_t, a_t, \mathcal{O}_{1:T})$

Recovering rationality using probabilistic graphical models for sub-optimal behaviour

Variational inference leads to obtaining an approximation $\hat{p}(s_{1:T}, a_{1:T})$ of $p(s_{1:T}, a_{1:T} | \mathcal{O}_{1:T})$ with dynamics $p(s_{t+1} | s_t, a_t)$. Let

$$\hat{p}(s_{1:T}, a_{1:T}) = p(s_1) \prod_t p(s_{t+1}|s_t, a_t) \hat{p}(a_t|s_t)$$

It is proved that by setting the variational lower bound

$$logp(\mathcal{O}_{1:T}) \geq \mathbb{E}_{(s_{1:T}, a_{1:T}) \sim \hat{p}}\left[\sum_{t} r(s_t, a_t) - log\hat{p}(a_t|s_t)\right]$$

this translates to maximize the reward and action entropy:

$$logp(\mathcal{O}_{1:T}) \geq \sum_{t} \mathbb{E}_{(s_t, a_t) \sim \hat{p}}[r(s_t, a_t) + \mathcal{H}(\hat{p}(a_t|s_t)]$$

Recovering rationality using probabilistic graphical models for sub-optimal behaviour $^{10}\,$

$$logp(\mathcal{O}_{1:T}) \geq \sum_{t} \mathbb{E}_{(s_t, a_t) \sim \hat{p}}[r(s_t, a_t) + \mathcal{H}(\hat{p}(a_t|s_t)]$$

is optimized when $\hat{p}(a_t|s_t) \propto exp(Q(s_t, a_t))$ resulting into

$$\pi(a_t|s_t) = \hat{\rho}(a_t|s_t) = \exp(Q(s_t, a_t) - V(s_t))$$
$$V(s_t) = \log \int \exp(Q_t(s_t, a_t)) \, da_t$$

with the regular (unbiased) Bellman backup

$$Q_t(s,a) = r(s_t,a_t) + \mathbb{E}[V_{t+1}(s_{t+1})]$$

¹⁰Levine (2018) "RL and control as probabilistic inference: Tutorial and review"

The anatomy of DRL algorithms: Soft Q-Learning



Soft Actor Critic (T.Haarnooja et al., 2018)



$$D_{KL}(\pi_{\theta}(\mathsf{a}|s)||\frac{1}{Z}\exp(Q_{\phi}(s,\mathsf{a}))) = \mathbb{E}_{s}[\mathbb{E}_{\mathsf{a}\sim\pi_{\theta}}(s)[\log\pi_{\theta}(\mathsf{a}|s) - Q_{\phi}(s,\mathsf{a})]]$$

So far...

- Recovering rationality considering sub-optimal behaviour
- Incorporating MaxEnt terms in the RL objective
- Q-Learning and Soft Q-learning
- Soft Actor Critic

Policy Gradient Goal: $maxJ(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\sum_{t} r(s_{t}, a_{t})] \approx \frac{1}{N} \sum_{i} \sum_{t} r(s_{i,t}, a_{i,t})$ $\nabla J(\theta) = \mathbb{E}_{\tau \sim \pi_{\theta}(\tau)} [(\sum_{t} \nabla_{\theta} log \pi_{\theta}(a_{t}|s_{t}))(\sum_{t} r(s_{t}, a_{t}))]$ $\nabla J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} (\sum_{t} \nabla_{\theta} log \pi_{\theta}(a_{t}|s_{t}))(\sum_{t} r(s_{t}, a_{t}))$ $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

REINFORCE Algorithm:

- 1. sample τ_i from $\pi_{\theta}(a_t|s_t)$
- 2. $\nabla J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} (\sum_{t} \nabla_{\theta} \log \pi_{\theta}(a_{t}|s_{t})) (\sum_{t} r(s_{t}, a_{t}))$
- 3. $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

4. Go to 1.

Policy Gradient with Causality and baselines

1. sample
$$\tau_i$$
 from $\pi_{\theta}(a_t|s_t)$

- 2. $\nabla J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} (\sum_{t} \nabla_{\theta} \log \pi_{\theta}(a_{t}|s_{t})) (\sum_{t} r(s_{t}, a_{t}))$
- 3. $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

4. Go to 1.

where

Reward to go:
$$\hat{Q}(s_t, a_t) = \sum_{t'=t}^{T} \mathbb{E}_{\pi_{\theta}}[r(s_{t'}, a_{t'}|s_t, a_t)]$$

It can simply be: $\hat{Q}(s_t, a_t) = \sum_{t'=t}^{T} r(s_t, a_t)$

and

Baseline:
$$b = V(s_t) = \mathbb{E}_{a_t \sim \pi_\theta(a_t|s_t)}[Q(s_t, a_t)]$$

It can simply be: $b = \frac{1}{N} \sum_i \hat{Q}(s_t^i, a_t^i)$

Policy Gradient with Causality and baselines

Reward to go:
$$Q(s_t, a_t) \approx \sum_{t'=t}^{T} \mathbb{E}_{\pi_{\theta}}[r(s_{t'}, a_{t'}|s_t, a_t)]$$

Baseline:
$$b = V(s_t) = \mathbb{E}_{a_t \sim \pi_{\theta}(a_t|s_t)}[Q(s_t, a_t)]$$

Advantage: $A(s_t, a_t) = Q(s_t, a_t) - V(s_t)$ Usually, a simple fit $\hat{A}(s_t, a_t)$ suffices. So,

1. sample
$$\tau_i$$
 from $\pi_{\theta}(a_t|s_t)$
2. $\nabla J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} (\sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i|s_t^i)) \hat{A}(s_t^i, a_t^i)$
3. $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$
4. Go to 1.

Policy Gradient with Causality and baselines and Importance sampling

Making the algorithm off-policy (i.e. exploit samples from previous iteration):

$$\nabla J(\theta) = \mathbb{E}_{\tau \sim \pi_{\theta}(\tau)} \left[\sum_{t} \nabla_{\theta} \log \pi_{\theta}(a_{t}|s_{t}) (\sum_{t} r(s_{t}, a_{t})) \right] = \mathbb{E}_{\tau \sim \pi_{\theta'}(\tau)} \left[\sum_{t} \frac{\pi_{\theta}(a_{t}|s_{t})}{\pi_{\theta'}(a_{t}|s_{t})} \nabla_{\theta} \log \pi_{\theta}(a_{t}|s_{t}) (\sum_{t} r(s_{t}, a_{t})) \right]$$

The Algorithm:

1. sample
$$\tau_i$$
 from $\pi_{\theta'}(a_t|s_t)$
2. $\nabla J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \left(\sum_t \frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta'}(a_t|s_t)} \nabla_{\theta} \log \pi_{\theta}(a_t^i|s_t^j) \right) \hat{A}(s_t^i, a_t^i)$
3. $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$
4. Go to 1.

Policy Gradient with Causality and baselines and Importance sampling

The Algorithm:

1. sample τ_i from $\pi_{\theta'}(a_t|s_t)$ 2. $\nabla J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \left(\sum_t \frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta'}(a_t|s_t)} \nabla_{\theta} \log \pi_{\theta}(a_t^i|s_t^i) \right) \hat{A}(s_t^i, a_t^i)$ 3. $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$ 4. Go to 1.



Trust Region Policy Optimization (TRPO) J.Schulman et al., "Trust Region Policy Optimization", 2015

$$\begin{array}{ll} \underset{\theta}{\mathsf{maximize}} & \hat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(a_t \mid s_t)}{\pi_{\theta_{\mathrm{old}}}(a_t \mid s_t)} \hat{A}_t \right] \\ \\ \text{subject to} & \hat{\mathbb{E}}_t [\mathsf{KL}[\pi_{\theta_{\mathrm{old}}}(\cdot \mid s_t), \pi_{\theta}(\cdot \mid s_t)]] \leq \delta \end{array}$$

Also worth considering using a penalty instead of a constraint

$$\underset{\theta}{\mathsf{maximize}} \qquad \hat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(a_t \mid s_t)}{\pi_{\theta_{\text{old}}}(a_t \mid s_t)} \hat{A}_t \right] - \beta \hat{\mathbb{E}}_t [\mathsf{KL}[\pi_{\theta_{\text{old}}}(\cdot \mid s_t), \pi_{\theta}(\cdot \mid s_t)]]$$

Introduction to (Deep) Reinforcement Learning Proximal Policy Optimization (PPO)

J.Schulman et al., "Proximal Policy Optimization", 2017

Input: initial policy parameters θ_0 , clipping threshold ϵ for k = 0, 1, 2, ... do Collect set of partial trajectories \mathcal{D}_k on policy $\pi_k = \pi(\theta_k)$ Estimate advantages $\hat{A}_t^{\pi_k}$ using any advantage estimation algorithm Compute policy update $\theta_{k+1} = \arg \max \mathcal{L}_{\theta_k}^{CLP}(\theta)$

by taking
$${\it K}$$
 steps of minibatch SGD (via Adam), where

$$\mathcal{L}^{\textit{CLIP}}_{\theta_k}(\theta) = \mathop{\mathbb{E}}_{\tau \sim \pi_k} \left[\sum_{t=0}^T \left[\min(r_t(\theta) \hat{A}^{\pi_k}_t, \mathsf{clip}\left(r_t(\theta), 1-\epsilon, 1+\epsilon\right) \hat{A}^{\pi_k}_t) \right] \right]$$

end for

where $r_t(\theta) = \pi_{\theta}(a_t|s_t)/\pi_{\theta_k}(a_t|s_t)$

- Clipping prevents policy from having incentive to go far away from θ_{k+1}

- Clipping seems to work at least as well as PPO with KL penalty, but is simpler to implement

In this last part of the DRL intro we addressed...

- Policy Gradient (addressing variance and bias)
- Importance sampling for sample efficiency
- Natural Policy Gradient (TRPO)
- Proximal Policy Optimization (PPO)